



# SLN DEGREE COLLEGE

Alamur Road, Anantapuramu

Affiliated to S.K. University

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## Department of Mathematics

The Department of Mathematics was started in the year 2016 with an UG Courses B.Sc (Maths, Statistics, and Computer Science), B.Sc (Maths, Physics, and Computer Science), B.Sc (Maths, Electronics, and Computer Science) was introduced.

The department is having well qualified and experienced faculty members. The faculty is a perfect blend of different specializations in Mathematics and applications to impart their expertise in handling diversified courses of the UG programs. The teaching methodology in the department goes beyond fulfilling the syllabus requirements of the University, to meet the today's industry needs. Faculty motivates and guides the students to do mini projects in core subjects. Special focus will be given to develop Communication and Soft Skills. The Department adopted and made the ICT in teaching techniques effectively.

### Mission

- To be a leading Mathematics Department in the country.
- To emerge as a global center of learning, academic excellence, and innovative research.

### Vision

- Imparting of quality mathematics education and the inculcating of the spirit of research through innovative teaching and research methodologies.
- To achieve high standards of excellence in generating and propagating knowledge in Mathematics. Department is committed to providing an education that combines rigorous academics with joy of discovery.
- To provide an environment where students can learn, become competent users of mathematics, and understand the use of mathematics in other disciplines.

**Courses / Programs offered:**

<b>Level</b>	<b>Course</b>
<b>UG</b>	B.Sc (MSCs)- Maths, Stats, Computer Science
	B.Sc (MPCs)- Maths, Physics, Computer Science
	B.Sc (MECs)- Maths, Electronics, Computer Science

## HOD profile

### 1. Personal details:

- a. Name of the Faculty :** U.V.RAMI REDDY  
**b. Department :** MATHEMATICS  
**c. Designation :** Asst.Professor (Selection Grade)  
**d. Subjects Taught :** Mathematics at Graduate level.

Abstract Algebra&Abstract Algebra Problem Solving Sessions

Real Analysis & Real Analysis. Problem Solving Sessions Ring Theory & Vector  
Calculus & Ring Theory & Vector Calculus, Problem Solving Sessions , Linear  
Algebra& Linear Algebra Problem Solving Sessions

**a. Level of Guidance & Teaching : -**

**b. Qualification: M.Sc., B.Ed,**

**c. Teaching Experience :** Graduate level : 25 years,  
Intermediate Level : 10 Years.

**d. Academic Degrees:**

Degree	University/Board	Date/ Year	Awarded/Grade/Class
B.Ed.,	Yogi Vemana University, KADAPA	2012	First Class
M.Sc.,(Maths)	Alagappa University,	2003	First Class
B.Sc., (M.P.Cs)	Govt. Arts College, Anantapur	1996	Distinction
Intermediate	BIE, Andhra Pradesh	1993	Distinction
S.S.C.	Board of Secondary School Education, AP	1991	First Class

### Faculty profile

Name	Qualification	Designation	Teaching Experience
Dr.Irfana	M.Sc., PhD.,	Asst. Professor	10
Mallesh	M.Sc.,	Asst. Professor	5

**Student profile Program wise:**

Name of the course	Year	Total Seats	Enrolled	<b>Total</b>
<b>Bsc (M.P.Cs)</b>				
<b>Bsc (M.S.Cs)</b>				
<b>Bsc (M.E.Cs)</b>				

**Infrastructure facilities:**

**Library:** There is a central library to cater to the need of the students. Department does not have a library. But the complimentary copies provided by different publisher are provided in the department for the use of the student.

**Internet facility for staff and students:** Yes (only for staff )

Classroom with ICT facility:

Yes Laboratories: Yes. Department has one single lab

**Course Structure under CBCS:**



**SRI KRISHNADEVARAYA UNIVERSITY:: ANANTAPURAMU**

**UG CBCS SYLLABUS  
VI Semester(2017-2018)**

**B.Sc., MATHEMATICS  
VI SEMESTER- SYLLABUS  
(AS PER CBCS AND SEMESTER  
SYSTEM)III YEARS**

**w.e.f. 2017-2018**



**AP STATE COUNCIL OF HIGHER  
EDUCATIONCBCS - PATTERN FOR  
MATHEMATICS**



	VIII	<i>work or</i> VIII-B-1: Principles of Mechanics VIII-B-2: Fluid Mechanics VIII-B-3: <i>Project work</i> or VIII-C-1: Graph Theory VIII-C-2: Applied Graph Theory VIII-C-3: <i>Project work</i>					
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**SRI KRISHNADEVARAY UNIVERSITY:: ANANTAPURAMUUG CBCS SYLLABUS**  
**B.A./B.Sc. THIRD YEAR MATHEMATICS SYLLABUS**  
**SEMESTER – VI, PAPER – VII-(A) ELECTIVE-VII(A); LAPLACE**  
**TRANSFORMS**

**UNIT – 1 (12 hrs) Laplace Transform I : - 60 Hrs**

Definition of - Integral Transform – Laplace Transform Linearity, Property, Piecewise continuous Functions, Existence of Laplace Transform, Functions of Exponential order, and of Class A.

**UNIT – 2 (12 hrs) Laplace Transform II : -**

First Shifting Theorem, Second Shifting Theorem, Change of Scale Property, Laplace Transform of the derivative of  $f(t)$ , Initial Value theorem and Final Value theorem.

**UNIT – 3 (12 hrs) Laplace Transform III : -**

Laplace Transform of Integrals – Multiplication by  $t$ , Multiplication by  $t^n$  – Division by  $t$ . Laplace transform of Bessel Function, Laplace Transform of Error Function, Laplace Transform of Sine and cosine integrals.

**UNIT – 4 (12 hrs) Inverse Laplace Transform I : -**

Definition of Inverse Laplace Transform. Linearity, Property, First Shifting Theorem, Second Shifting Theorem, Change of Scale property, use of partial fractions, Examples.

**UNIT – 5 (12 hrs) Inverse Laplace Transform II : -**

Inverse Laplace transforms of Derivatives–Inverse Laplace Transforms of Integrals – Multiplication by Powers of ‘ $P$ ’– Division by powers of ‘ $P$ ’– Convolution Definition – Convolution Theorem – proof and Applications – Heaviside’s Expansion theorem and its Applications.

**Reference Books :-**

1. Laplace Transforms by A.R. Vasistha and Dr. R.K. Gupta Published by Krishna Prakashan Media Pvt. Ltd. Meerut.
2. Fourier Series and Integral Transforms by Dr. S. Sreenadh Published by S.Chand and Co., Pvt. Ltd., New Delhi.
3. Laplace and Fourier Transforms by Dr. J.K. Goyal and K.P. Gupta, Published by Pragathi Prakashan, Meerut.
4. Integral Transforms by M.D. Raising hania, - H.C. Saxsena and H.K. Dass Published by S. Chandand Co., Pvt.Ltd., New Delhi.

**Suggested Activities:**

Seminar/ Quiz/ Assignments



**B.A./B.Sc. THIRD YEAR MATHEMATICS SYLLABUS, SEMESTER – VI,  
CLUSTER – A, PAPER – VIII-A-1  
Cluster Elective- VIII-A-1: INTEGRAL TRANSFORMS**

**UNIT – 1 (12 hrs) Application of Laplace Transform to solutions of Differential Equations :-**

Solutions of ordinary Differential Equations.

Solutions of Differential Equations with constants co-efficient  
Solutions of Differential Equations with Variable co-efficient

**UNIT – 2 (12 hrs) Application of Laplace Transform :-** Solution of simultaneous ordinary Differential Equations. Solutions of partial Differential Equations.

**UNIT – 3 (12 hrs) Application of Laplace Transforms to Integral Equations :- 60 Hrs**

**Definitions :** Integral Equations-Abel's, Integral Equation-Integral Equation of Convolution Type, Integro Differential Equations. Application of L.T. to Integral Equations.

**UNIT – 4 (12 hrs) Fourier Transforms-I :-**

Definition of Fourier Transform – Fourier's in Transform – Fourier cosine Transform – Linear Property of Fourier Transform – Change of Scale Property for Fourier Transform – sine Transform and cosine transform shifting property – modulation theorem.

**UNIT – 5 (12 hrs) Fourier Transform-II :-**

Convolution Definition – Convolution Theorem for Fourier transform – parseval's Identify – Relationship between Fourier and Laplace transforms – problems related to Integral Equations.

**Finte Fourier Transforms :-**

Finte Fourier Sine Transform – Finte Fourier Cosine Transform – Inversion formula for sine and cosine Transforms only statement and related problems.

**Reference Books :-**

1. Integral Transforms by A.R. Vasistha and Dr. R.K. Gupta Published by Krishna Prakashan Media Pvt. Ltd. Meerut.
2. A Course of Mathematical Analysis by Shanthi Narayana and P.K. Mittal, Published by S. Chand and Company pvt. Ltd., New Delhi.
3. Fourier Series and Integral Transforms by Dr. S. Sreenadh Published by S.Chand and Company Pvt. Ltd., New Delhi.
4. Lapalce and Fourier Transforms by Dr. J.K. Goyal and K.P. Gupta, Published by Pragathi Prakashan, Meerut.
5. Integral Transforms by M.D. Raising hania, - H.C. Saxsena and H.K. Dass Published by S.Chand and Company pvt. Ltd., New Delhi.

**Suggested Activities:**

Seminar/ Quiz/ Assignments

**SRI KRISHNADEVARAY UNIVERSITY:: ANANTAPURAMUUG CBCS  
SYLLABUS**

**B.A./B.Sc. THIRD YEAR MATHEMATICS SYLLABUS SEMESTER –  
VI: PAPER – VIII-A-2**

**ELECTIVE – VIII-A-2: ADVANCED NUMERICAL ANALYSIS**

**Unit – I (10 Hours) 60 Hrs Curve Fitting:** Least – Squares curve fitting procedures, fitting a straight line, nonlinear curve fitting, Curve fitting by a sum of exponentials.

**UNIT- II : (12 hours)**

**Numerical Differentiation:** Derivatives using Newton’s forward difference formula, Newton’s backward difference formula, Derivatives using central difference formula, Stirling’s interpolation formula, Newton’s divided difference formula, Maximum and minimum values of a tabulated function.

**UNIT- III : (12 hours)**

**Numerical Integration:** General quadrature formula on errors, Trapezoidal rule, Simpson’s 1/3 – rule, Simpson’s 3/8 – rule, and Weddle’s rules, Euler – Maclaurin Formula of summation and quadrature, The Euler transformation.

**UNIT – IV: (14 hours)**

**Solutions of simultaneous Linear Systems of Equations:** Solution of linear systems – Direct methods, Matrix inversion method, Gaussian elimination methods, Gauss-Jordan Method, Method of factorization, Solution of Tridiagonal Systems, Iterative methods. Jacobi’s method, Gauss-Seidel method.

**UNIT – V (12 Hours)**

**Numerical solution of ordinary differential equations:** Introduction, Solution by Taylor’s Series, Picard’s method of successive approximations, Euler’s method, Modified Euler’s method, Runge – Kutta methods.

**Reference Books :**

1. Numerical Analysis by S.S.Sastry, published by Prentice Hall India (Latest Edition).
2. Numerical Analysis by G. Sankar Rao, published by New Age International Publishers, New – Hyderabad.
1. Finite Differences and Numerical Analysis by H.C Saxena published by S. Chand and Company, Pvt.Ltd., New Delhi.
4. Numerical methods for scientific and engineering computation by M.K.Jain, S.R.K.Iyengar, R.K. Jain.

**Suggested Activities:**

Seminar/ Quiz/ Assignments .

**SRI KRISHNADEVARAY UNIVERSITY:: ANANTAPURAMUUG CBCS  
SYLLABUS**

**B.A./B.Sc. THIRD YEAR MATHEMATICS SYLLABUS SEMESTER –  
VI: PAPER – VIII-A-3**

**ELECTIVE – VIII-A-3: PROJECT WORK**

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# ANDHRA PRADESH STATE COUNCIL OF HIGHER EDUCATION

(A Statutory body of the Government of Andhra Pradesh)

3<sup>rd</sup>, 4<sup>th</sup> and 5<sup>th</sup> floors, Neeladri Towers, Sri Ram Nagar, 6<sup>th</sup> Battalion Road,  
Atmakur(V), Mangalagiri(M), Guntur-522 503, Andhra Pradesh  
**Web:** [www.apsche.org](http://www.apsche.org) **Email:** [acapsche@gmail.com](mailto:acapsche@gmail.com)

## REVISED SYLLABUS OF B.A. /B.Sc. MATHEMATICS UNDER CBCS FRAMEWORK WITH EFFECT FROM 2020-2021

### **PROGRAMME: THREE-YEAR B.A. /B.Sc. MATHEMATICS**

*(With Learning Outcomes, Unit-wise Syllabus, References, Co-curricular Activities & Model Q.P.)*

*For Fifteen Courses of 1, 2, 3 & 4 Semesters)*

**(To be Implemented from 2020-21 Academic Year)**

**A.P. STATE COUNCIL OF HIGHER EDUCATION**

**B.A./B.Sc. MATHEMATICS**

**REVISED SYLLABUS FOR CORE COURSES**

**CBCS/ SEMESTER SYSTEM**

**(w.e.f. 2020-21 Admitted Batch)**

**CORE COURSES STRUCTURE**

**(Sem-I to Sem-IV)**

Course	Subject	Hrs.	Credits	IA	ES	Total
Course -I	Differential Equations & Differential Equations Problem Solving Sessions	6	5	25	75	100
Course -II	Three dimensional analytical Solid geometry & Three dimensional analytical Solid Geometry Problem Solving Sessions	6	5	25	75	100
Course -III	Abstract Algebra & Abstract Algebra Problem Solving Sessions	6	5	25	75	100
Course -IV	Real Analysis & Real Analysis Problem Solving Sessions	6	5	25	75	100
Course -V	Linear Algebra & Linear Algebra Problem Solving Sessions	6	5	25	75	100

**COURSE-I**  
**CBCS/ SEMESTER SYSTEM**  
**B.A./B.Sc. MATHEMATICS (w.e.f. 2020-21 Admitted Batch)**  
**DIFFERENTIAL EQUATIONS**  
**SYLLABUS (75 Hours)**

**Course Outcomes:**

After successful completion of this course, the student will be able to;

1. Solve linear differential equations
2. Convert non exact homogeneous equations to exact differential equations by using integrating factors.
3. Know the methods of finding solutions of differential equations of the first order but not of the first degree.
4. Solve higher-order linear differential equations, both homogeneous and non homogeneous, with constant coefficients.
5. Understand the concept and apply appropriate methods for solving differential equations.

**Course Syllabus:**

**UNIT – I (12 Hours)**

**Differential Equations of first order and first degree:**

Linear Differential Equations; Differential equations reducible to linear form; Exact differential equations; Integrating factors; Change of variables.

**UNIT – II (12 Hours)**

Orthogonal Trajectories

**Differential Equations of first order but not of the first degree:**

Equations solvable for  $p$ ; Equations solvable for  $y$ ; Equations solvable for  $x$ ; Equations that do not contain  $x$  (or  $y$ ); Equations homogeneous in  $x$  and  $y$ ; Equations of the first degree in  $x$  and  $y$  – Clairaut's Equation.

### UNIT – III (12 Hours)

#### Higher order linear differential equations-I:

Solution of homogeneous linear differential equations of order  $n$  with constant coefficients; Solution of the non-homogeneous linear differential equations with constant coefficients by means of polynomial operators. General Solution of  $f(D)y=0$ .

General Solution of  $f(D)y=Q$  when  $Q$  is a function of  $x$ ,

P.I. of  $f(D)y = Q$  when  $Q = be^{ax}$  \_\_\_\_\_

P.I. of  $f(D)y = Q$  when  $Q$  is  $b\sin ax$  or  $b \cos ax$ .  $f(D)$  is expressed as partial fractions.

### UNIT – IV (12 Hours)

#### Higher order linear differential equations-II:

Solution of the non-homogeneous linear differential equations with constant coefficients.

P.I. of  $f(D)y = Q$  when  $Q = bx^k$

P.I. of  $f(D)y = Q$  when  $Q = e^{ax}V$ , where  $V$  is a function of  $x$ .

P.I. of  $f(D)y = Q$  when  $Q = xV$ , where  $V$  is a function of  $x$ .

of  $f(D)y = Q$  when  $Q = x^mV$ , where  $V$  is a function of  $x$ .

### UNIT –V (12 Hours)

#### Higher order linear differential equations-III :

Method of variation of parameters; Linear differential Equations with non-constant coefficients; The Cauchy-Euler Equation, Legendre's linear equations, miscellaneous differential equations.

### Co-Curricular Activities(15 Hours)

Seminar/ Quiz/ Assignments/ Applications of Differential Equations to Real life Problem /Problem Solving.

#### Text Book :

Differential Equations and Their Applications by Zafar Ahsan, published by Prentice-Hall of India Pvt. Ltd, New Delhi-Second edition.

#### Reference Books :

1. A text book of Mathematics for B.A/B.Sc, Vol 1, by N. Krishna Murthy & others, published by S.Chand & Company, New Delhi.
2. Ordinary and Partial Differential Equations by Dr. M.D,Raisinghanian, published by S. Chand &

Company, New Delhi.

3. Differential Equations with applications and programs – S. Balachandra Rao & HR Anuradha-  
Universities Press.

4. Differential Equations -Srinivas Vangala & Madhu Rajesh, published by Spectrum University  
Press.



**COURSE-II**  
**CBCS/ SEMESTER SYSTEM**  
**(w.e.f. 2020-21 Admitted**  
**Batch)B.A./B.Sc.**  
**MATHEMATICS**  
**THREE DIMENSIONAL ANALYTICAL SOLID GEOMETRY**  
**Syllabus (75 Hours)**

**Course Outcomes:**

After successful completion of this course, the student will be able to;

1. get the knowledge of planes.
2. basic idea of lines, sphere and cones.
3. understand the properties of planes, lines, spheres and cones.
4. express the problems geometrically and then to get the solution.

## **Course Syllabus:**

### **UNIT – I (12 Hours)**

Equation of plane in terms of its intercepts on the axis, Equations of the plane through the given points, Length of the perpendicular from a given point to a given plane, Bisectors of angles between two planes, Combined equation of two planes, Orthogonal projection on a plane.

### **UNIT – II (12 hrs)**

#### **The Line :**

Equation of a line; Angle between a line and a plane; The condition that a given line may lie in a given plane; The condition that two given lines are coplanar; Number of arbitrary constants in the equations of straight line; Sets of conditions which determine a line; The shortest distance between two lines; The length and equations of the line of shortest distance between two straight lines; Length of the perpendicular from a given point to a given line.

### **UNIT – III (12 hrs)**

#### **The Sphere :**

Definition and equation of the sphere; Equation of the sphere through four given points; Plane sections of a sphere; Intersection of two spheres; Equation of a circle; Sphere through a given circle; Intersection of a sphere and a line; Power of a point; Tangent plane; Plane of contact; Polar plane; Pole of a Plane; Conjugate points; Conjugate planes;

### **UNIT – IV (12 hrs)**

#### **The Sphere and Cones :**

Angle of intersection of two spheres; Conditions for two spheres to be orthogonal; Radical plane; Coaxial system of spheres; Simplified form of the equation of two spheres.

Definitions of a cone; vertex; guiding curve; generators; Equation of the cone with a given vertex and guiding curve; equations of cones with vertex at origin are homogenous; Condition that the general equation of the second degree should represent a cone;

## UNIT – V (12 hrs)

### **Cones :**

Enveloping cone of a sphere; right circular cone: equation of the right circular cone with a given vertex, axis and semi vertical angle: Condition that a cone may have three mutually perpendicular generators; intersection of a line and a quadric cone; Tangent lines and tangent plane at a point; Condition that a plane may touch a cone; Reciprocal cones; Intersection of two cones with a common vertex.

### **Co-Curricular Activities(15 Hours)**

Seminar/ Quiz/ Assignments/Three dimensional analytical Solid geometry and its applications/ Problem Solving.

### **Text Book :**

Analytical Solid Geometry by Shanti Narayan and P.K. Mittal, published by S. Chand & Company Ltd. 7th Edition.

### **Reference Books :**

1. A text book of Mathematics for BA/B.Sc Vol 1, by V Krishna Murthy & Others, published by S. Chand & Company, New Delhi.
2. A text Book of Analytical Geometry of Three Dimensions, by P.K. Jain and Khaleel Ahmed, published by Wiley Eastern Ltd., 1999.
3. Co-ordinate Geometry of two and three dimensions by P. Balasubrahmanyam, K.Y. Subrahmanyam, G.R. Venkataraman published by Tata-MC Gran-Hill Publishers Company Ltd., New Delhi.
4. Solid Geometry by B.Rama Bhupal Reddy, published by Spectrum University Press.

**COURSE-III**  
**CBCS/ SEMESTER SYSTEM**  
**(w.e.f. 2020-21 Admitted**  
**Batch)B.A./B.Sc.**  
**MATHEMATICS**  
**ABSTRACT ALGEBRA**  
**SYLLABUS (75 Hours)**

**Course Outcomes:**

After successful completion of this course, the student will be able to;

1. acquire the basic knowledge and structure of groups, subgroups and cyclic groups.
2. get the significance of the notation of a normal subgroups.
3. get the behavior of permutations and operations on them.
4. study the homomorphisms and isomorphisms with applications.
5. understand the ring theory concepts with the help of knowledge in group theory and to prove the theorems.
6. understand the applications of ring theory in various fields.

## **Course Syllabus:**

### **UNIT – I (12 Hours)**

#### **GROUPS :**

Binary Operation – Algebraic structure – semi group-monoid – Group definition and elementary properties Finite and Infinite groups – examples – order of a group, Composition tables with examples.

### **UNIT – II (12 Hours)**

#### **SUBGROUPS :**

Complex Definition – Multiplication of two complexes Inverse of a complex-Subgroup definition- examples-criterion for a complex to be a subgroups. Criterion for the product of two subgroups to be a subgroup-union and Intersection of subgroups.

#### **Co-sets and Lagrange's Theorem :**

Cosets Definition – properties of Cosets–Index of a subgroups of a finite groups–Lagrange's Theorem.

### **UNIT –III (12 Hours)**

#### **NORMAL SUBGROUPS :**

Definition of normal subgroup – proper and improper normal subgroup–Hamilton group – criterion for a subgroup to be a normal subgroup – intersection of two normal subgroups – Sub group of index 2 is a normal sub group –quotient group – criteria for the existence of a quotient group.

#### **HOMOMORPHISM :**

Definition of homomorphism – Image of homomorphism elementary properties of homomorphism – Isomorphism – automorphism definitions and elementary properties–kernel of a homomorphism – fundamental theorem on Homomorphism and applications.

### **UNIT – IV (12 Hours)**

#### **PERMUTATIONS AND CYCLIC GROUPS :**

Definition of permutation – permutation multiplication – Inverse of a permutation – cyclic permutations – transposition – even and odd permutations – Cayley's theorem.

**Cyclic Groups :-** Definition of cyclic group – elementary properties – classification of cyclic groups.

## **UNIT – V (12 Hours)**

### **RINGS :**

Definition of Ring and basic properties, Boolean Rings, divisors of zero and cancellation laws Rings, Integral Domains, Division Ring and Fields, The characteristic of a ring - The characteristic of an Integral Domain, The characteristic of a Field. Sub Rings, Ideals

### **Co-Curricular Activities(15 Hours)**

Seminar/ Quiz/ Assignments/ Group theory and its applications / Problem Solving.

### **Text Book :**

A text book of Mathematics for B.A. / B.Sc. by B.V.S.S. SARMA and others, published by S.Chand & Company, New Delhi.

### **Reference Books :**

1. Abstract Algebra by J.B. Fraleigh, Published by Narosa publishing house.
2. Modern Algebra by M.L. Khanna.
3. Rings and Linear Algebra by Pundir & Pundir, published by Pragathi Prakashan.

**COURSE-IV**  
**CBCS/ SEMESTER SYSTEM**  
**(w.e.f. 2020-21 Admitted Batch)**  
**B.A./B.Sc. MATHEMATICS REAL**  
**ANALYSIS**  
**SYLLABUS (75 Hours)**

**Course Outcomes:**

After successful completion of this course, the student will be able to

1. get clear idea about the real numbers and real valued functions.
2. obtain the skills of analyzing the concepts and applying appropriate methods for testing convergence of a sequence/ series.
3. test the continuity and differentiability and Riemann integration of a function.
4. know the geometrical interpretation of mean value theorems.

**Course Syllabus:**

**UNIT – I (12 Hours)**

**REAL NUMBERS :**

The algebraic and order properties of  $\mathbb{R}$ , Absolute value and Real line, Completeness property of  $\mathbb{R}$ , Applications of supremum property; intervals. (No question is to be set from this portion).

**Real Sequences:**

Sequences and their limits, Range and Boundedness of Sequences, Limit of a sequence and Convergent sequence. The Cauchy's criterion, properly divergent sequences, Monotone sequences, Necessary and Sufficient condition for Convergence of Monotone Sequence, Limit Point of Sequence, Subsequences and the Bolzano-weierstrass theorem – Cauchy Sequences – Cauchy's general principle of convergence theorem.

**UNIT –II (12 Hours)**

**INFINITIE SERIES :**

**Series** :Introduction to series, convergence of series. Cauchy's general principle of convergence for series tests for convergence of series, Series of Non-Negative Terms.

1. P-test
2. Cauchy's  $n^{\text{th}}$  root test or Root Test.
3. D'Alemberts' Test or Ratio Test.
4. Alternating Series – Leibnitz Test.

Absolute convergence and conditional convergence.

### **UNIT – III (12 Hours)**

#### **CONTINUITY :**

**Limits :** Real valued Functions, Boundedness of a function, Limits of functions. Some extensions of the limit concept, Infinite Limits. Limits at infinity. (No question is to be set from this portion).

**Continuous functions :** Continuous functions, Combinations of continuous functions, Continuous Functions on intervals, uniform continuity.

### **UNIT – IV (12 Hours)**

#### **DIFFERENTIATION AND MEAN VALUE THEORMS :**

The derivability of a function, on an interval, at a point, Derivability and continuity of a function, Graphical meaning of the Derivative, Mean value Theorems; Rolle's Theorem, Lagrange's Theorem, Cauchy's Mean value Theorem

### **UNIT – V (12 Hours)**

#### **RIEMANN INTEGRATION :**

Riemann Integral, Riemann integral functions, Darboux theorem. Necessary and sufficient condition for R – integrability, Properties of integrable functions, Fundamental theorem of integral calculus, integral as the limit of a sum, Mean value Theorems.

### **Co-Curricular Activities(15 Hours)**

Seminar/ Quiz/ Assignments/ Real Analysis and its applications / Problem Solving.

#### **Text Book:**

Introduction to Real Analysis by Robert G.Bartle and Donlad R. Sherbert, published by John Wiley.

#### **Reference Books:**

- 1.A Text Book of B.Sc Mathematics by B.V.S.S. Sarma and others, published by S. Chand & Company Pvt. Ltd., New Delhi.
- 2.Elements of Real Analysis as per UGC Syllabus by Shanthi Narayan and Dr. M.D. Raisinghanian, published by S. Chand & Company Pvt. Ltd., New Delhi.



**COURSE-V**  
**CBCS/ SEMESTER SYSTEM**  
**(w.e.f. 2020-21 Admitted**  
**Batch)B.A./B.Sc.**  
**MATHEMATICS**  
**LINEAR ALGEBRA**  
**SYLLABUS (75 Hours)**

**Course Outcomes:**

After successful completion of this course, the student will be able to;

1. understand the concepts of vector spaces, subspaces, bases, dimension and their properties
2. understand the concepts of linear transformations and their properties
3. apply Cayley- Hamilton theorem to problems for finding the inverse of a matrix and higher powers of matrices without using routine methods
4. learn the properties of inner product spaces and determine orthogonality in inner product spaces.

**Course Syllabus:**

**UNIT – I (12 Hours)**

**Vector Spaces-I:**

Vector Spaces, General properties of vector spaces, n-dimensional Vectors, addition and scalar multiplication of Vectors, internal and external composition, Null space, Vector subspaces, Algebra of subspaces, Linear Sum of two subspaces, linear combination of Vectors, Linear span Linear independence and Linear dependence of Vectors.

**UNIT –II (12 Hours)**

**Vector Spaces-II:**

Basis of Vector space, Finite dimensional Vector spaces, basis extension, co-ordinates, Dimension of a Vector space, Dimension of a subspace, Quotient space and Dimension of Quotient space.

**UNIT –III (12 Hours)**

**Linear Transformations:**

Linear transformations, linear operators, Properties of L.T, sum and product of LTs, Algebra of Linear Operators, Range and null space of linear transformation, Rank and Nullity of linear transformations – Rank – Nullity Theorem.

## **UNIT –IV (12 Hours)**

### **Matrix :**

Matrices, Elementary Properties of Matrices, Inverse Matrices, Rank of Matrix, Linear Equations, Characteristic equations, Characteristic Values & Vectors of square matrix, Cayley – Hamilton Theorem.

## **UNIT –V (12 Hours)**

### **Inner product space :**

Inner product spaces, Euclidean and unitary spaces, Norm or length of a Vector, Schwartz inequality, Triangle Inequality, Parallelogram law, Orthogonality, Orthonormal set, complete orthonormal set, Gram – Schmidt orthogonalisation process. Bessel's inequality and Parseval's Identity.

## **Co-Curricular Activities(15 Hours)**

Seminar/ Quiz/ Assignments/ Linear algebra and its applications / Problem Solving.

### **Text Book:**

Linear Algebra by J.N. Sharma and A.R. Vasista, published by Krishna Prakashan Mandir, Meerut- 250002.

### **Reference Books :**

1. Matrices by Shanti Narayana, published by S.Chand Publications.
2. Linear Algebra by Kenneth Hoffman and Ray Kunze, published by Pearson Education (low priced edition), New Delhi.
3. Linear Algebra by Stephen H. Friedberg et. al. published by Prentice Hall of India Pvt. Ltd. 4<sup>th</sup> Edition, 2007.

**Recommended Question Paper Patterns and  
Models BLUE PRINT FOR QUESTION  
PAPER PATTERN COURSE-I,  
DIFFERENTIAL EQUATIONS**

<b>Unit</b>	<b>TOPIC</b>	<b>S.A.Q(including choice)</b>	<b>E.Q(including choice)</b>	<b>Total Marks</b>
<b>I</b>	Differential Equations of 1 <sup>st</sup> order and 1 <sup>st</sup> degree	2	2	30
<b>II</b>	Orthogonal Trajectories, Differential Equations of 1 <sup>st</sup> order but not of 1 <sup>st</sup> degree	2	2	30
<b>III</b>	Higher Order Linear Differential Equations (with constant coefficients) – I	1	2	25
<b>IV</b>	Higher Order Linear Differential Equations (with constant coefficients) – II	2	2	30
<b>V</b>	Higher Order Linear Differential Equations (with non constant coefficients)	1	2	25
<b>TOTAL</b>		8	10	140

**S.A.Q.** = Short answer questions (5 marks)

**E.Q.** = Essay questions (10 marks)

Short answer questions : 5 X 5 M = 25 M

Essay questions : 5 X 10 M = 50 M

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Total Marks = 75 M  
.....

**CBCS/ SEMESTER SYSTEM**  
**(W.e.f 2020-21 Admitted Batch)**  
**B.A./B.Sc. MATHEMATICS**  
**COURSE-I, DIFFERENTIAL EQUATIONS**  
**MATHEMATICS MODEL PAPER**

**Time: 3Hrs**

**Max.Marks:75M**

**SECTION - A**

**Answer any FIVE questions. Each question carries FIVE marks 5 X 5 M=25 M**

1. Solve  $(1 + e^{x/y}) dx + e^{x/y} (1 - x) dy = 0$ .
2. Solve  $(y - e^{\sin^{-1} x}) \frac{dx}{dy} + \sqrt{1 - x^2} = 0$
3. Solve  $y + px = p^2 x^4$ .
4. Solve  $(px - y)(py + x) = 2p$
5. Solve  $(D^2 - 3D + 2)y = \cosh x$
6. Solve  $(D^2 - 4D + 3)y = \sin 3x \cos 2x$ .
7. Solve  $\frac{d^2 y}{dx^2} - 6 \frac{dy}{dx} + 13y = 8e^{3x} \sin 2x$ .
8. Solve  $x^2 y'' - 2x(1 + x)y' + 2(1 + x)y = x^3$

**SECTION - B**

**Answer ALL the questions. Each question carries TEN marks. 5 X 10 M = 50 M**

9 a) Solve  $x \frac{dy}{dx} + y = y^2 \log x$ .

(Or)

9 b) Solve  $(y + \frac{1}{3}y^3 + \frac{1}{2}x^2) dx + \frac{1}{4}(x + xy^2) dy = 0$ .

10 a) Solve  $pe^{2x} + 2p^2 y \cot x = y^2$ .

(Or)

10 b) Find the orthogonal trajectories of the family of curves  $x^{2/3} + y^{2/3} = a^{2/3}$  where 'a' is the parameter.

11 a) Solve  $(D^3 + D^2 - D - 1)y = \cos 2x$ . 11 b) Solve  $(D^2 - 3D + 2)y = \sin e^{-x}$ .

(Or)

12 a) Solve  $(D^2 - 2D + 4)y = 8(x^2 + e^{2x} + \sin 2x)$

(Or)

12 b)  $\frac{d^2y}{dx^2} + 3\frac{dy}{dx} + 2y = xe^x \sin x$

13

a) Solve  $(D^2 - 2D)y = e^x \sin x$  by the method of variation of parameters.

(Or)

13 b) Solve  $3x^2 \frac{d^2y}{dx^2} + x \frac{dy}{dx} + y = x$

**BLUE PRINT FOR QUESTION PAPER PATTERN**  
**COURSE-II, THREE DIMENSIONAL ANALYTICAL SOLID GEOMETRY**

<b>Unit</b>	<b>TOPIC</b>	<b>S.A.Q(including choice)</b>	<b>E.Q(including choice)</b>	<b>Total Marks</b>
<b>I</b>	The Plane	2	2	30
<b>II</b>	The Right Line	2	2	30
<b>III</b>	The Sphere	2	2	30
<b>IV</b>	The Sphere & The Cone	1	2	25
<b>V</b>	The Cone	1	2	25
<b>TOTAL</b>		8	10	140

**S.A.Q.** = Short answer questions (5 marks)

**E.Q.** = Essay questions (10 marks)

Short answer questions : 5 X 5 M = 25 M

Essay questions : 5 X 10 M = 50 M

.....  
Total Marks = 75 M

.....

## CBCS/ SEMESTER SYSTEM

(w.e.f. 2020-21 Admitted Batch)

B.A./B.Sc. MATHEMATICS

### COURSE-II, THREE DIMENSIONAL ANALYTICAL SOLID GEOMETRY

Time: 3Hrs

Max.Marks:75 M

#### SECTION - A

Answer any **FIVE** questions. Each question carries **FIVE** marks 5 X 5 M=25 M

1. Find the equation of the plane through the point (-1,3,2) and perpendicular to the planes  $x+2y+2z=5$  and  $3x+3y+2z=8$ .
2. Find the bisecting plane of the acute angle between the planes  $3x-2y-6z+2=0$ ,  $-2x+y-2z-2=0$ .
3. Find the image of the point (2,-1,3) in the plane  $3x-2y+z=9$ .
4. Show that the lines  $2x + y - 4 = 0 = y + 2z$  and  $x + 3z - 4 = 0$ ,  $2x + 5z - 8 = 0$  are coplanar.
5. A variable plane passes through a fixed point (a, b, c). It meets the axes in A,B,C. Show that the centre of the sphere OABC lies on  $ax^{-1}+by^{-1}+cz^{-1}=2$ .
6. Show that the plane  $2x-2y+z+12=0$  touches the sphere  $x^2+y^2+z^2-2x-4y+2z-3=0$  and find the point of contact.
7. Find the equation to the cone which passes through the three coordinate axes and the lines  $\frac{x}{1} = \frac{y}{-2} = \frac{z}{3}$  and  $\frac{x}{2} = \frac{y}{1} = \frac{z}{1}$
8. Find the equation of the enveloping cone of the sphere  $x^2 + y^2 + z^2 + 2x - 2y = 2$  with its vertex at (1, 1, 1).

#### SECTION - B

Answer **ALL** the questions. Each question carries **TEN** marks. 5 X 10 M = 50 M

9(a) A plane meets the coordinate axes in A, B, C. If the centroid of  $\Delta ABC$  is

(a,b,c), show that the equation of the plane is  $\frac{x}{a} + \frac{y}{b} + \frac{z}{c} = 3$ .

(OR)

(b) A variable plane is at a constant distance p from the origin and meets the axes in A,B,C. Show that the locus of the centroid of the tetrahedron OABC is

$$x^2+y^2+z^2=16p^2.$$

10(a) Find the shortest distance between the lines

$$\frac{x-3}{3} = \frac{y-8}{-1} = \frac{z-3}{1}; \quad \frac{x+3}{-3} = \frac{y+7}{2} = \frac{z-6}{4}.$$

(OR)

(b) Prove that the lines  $\frac{x-1}{2} = \frac{y-2}{3} = \frac{z-3}{4}; \frac{x-2}{3} = \frac{y-3}{4} = \frac{z-4}{5}$  are coplanar. Also find their point of intersection and the plane containing the lines.

11 (a) Show that the two circles  $x^2+y^2+z^2-y+2z=0$ ,  $x-y+z=2$ ;

$x^2+y^2+z^2+x-3y+z-5=0$ ,  $2x-y+4z-1=0$  lie on the same sphere and find its equation.

(OR)

(b) Find the equation of the sphere which touches the plane  $3x+2y-z+2=0$  at  $(1,-2,1)$  and cuts orthogonally the sphere  $x^2+y^2+z^2-4x+6y+4=0$ .

12 (a) Find the limiting points of the coaxial system of spheres

$$x^2+y^2+z^2-8x+2y-2z+32=0, \quad x^2+y^2+z^2-7x+z+23=0.$$

(OR)

(b) Find the equation to the cone with vertex is the origin and whose base curve is  $x^2+y^2+z^2+2ux+d=0$ .

13 (a) Prove that the equation  $\sqrt{fx} \pm \sqrt{gy} \pm \sqrt{hz} = 0$  represents a cone that touches the coordinate planes and find its reciprocal cone.

(OR)

(b) Find the equation of the sphere  $x^2+y^2+z^2-2x+4y-1=0$  having its generators parallel to the line  $x=y=z$ .



**BLUE PRINT FOR QUESTION PAPER**  
**PATTERN COURSE-III, ABSTRACT**  
**ALGEBRA**

<b>Unit</b>	<b>TOPIC</b>	<b>S.A.Q(including choice)</b>	<b>E.Q(including choice)</b>	<b>Total Marks</b>
I	Groups	2	2	30
II	Subgroups, Cosets & Lagrange's theorem	1	2	25
III	Normal Subgroups and Homomorphism	1	2	25
IV	Permutations and Cyclic groups	2	2	30
V	Rings	2	2	30
Total		8	10	140

**S.A.Q.** = Short answer questions (5 marks)

**E.Q.** = Essay questions (10 marks)

Short answer questions : 5 X 5 M = 25 M

Essay questions : 5 X 10 M = 50 M

.....  
Total Marks = 75 M  
.....

**CBCS/ SEMESTER SYSTEM**  
(w.e.f. 2020-21 Admitted Batch)  
**B.A./B.Sc. MATHEMATICS**  
**COURSE-III, ABSTRACT ALGEBRA**

Time: 3Hrs

Max.Marks:75M

**SECTION - A**

Answer any **FIVE** questions. Each question carries **FIVE** marks 5 X 5 M=25 M

1. Show that the set  $G = \{x/x = 2^a 3^b \text{ and } a, b \in \mathbb{Z}\}$  is a group under multiplication
2. Define order of an element. In a group G, prove that if  $a \in G$  then  $O(a) = O(a)^{-1}$ .
3. If H and K are two subgroups of a group G, then prove that  $HK$  is a subgroup  $\Leftrightarrow HK=KH$
4. If G is a group and H is a subgroup of index 2 in G then prove that H is a normal subgroup.
5. Examine whether the following permutations are even or odd

i) 
$$\begin{pmatrix} 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 \\ 6 & 1 & 4 & 3 & 2 & 5 & 7 & 8 & 9 \end{pmatrix}$$

ii) 
$$\begin{pmatrix} 1 & 2 & 3 & 4 & 5 & 6 & 7 \\ 2 & 3 & 4 & 5 & 6 & 7 & 1 \end{pmatrix}$$

6. Prove that a group of prime order is cyclic.
7. Prove that the characteristic of an integral domain is either prime or zero.
8. If F is a field then prove that  $\{0\}$  and F are the only ideals of F.

**SECTION - B**

Answer **ALL** the questions. Each question carries **TEN** marks. 5 X 10 M = 50 M

9 a) Show that the set of  $n^{\text{th}}$  roots of unity forms an abelian group under multiplication.

(Or)

9 b) In a group G, for  $a, b \in G$ ,  $O(a)=5$ ,  $b \neq e$  and  $aba^{-1} = b^2$ . Find  $O(b)$ .

10 a) The Union of two subgroups is also a subgroup  $\Leftrightarrow$  one is contained in the other.

(Or)

b) State and prove Lagrange's theorem.

11 a) Prove that a subgroup  $H$  of a group  $G$  is a normal subgroup of  $G$  iff the product of two right cosets of  $H$  in  $G$  is again a right coset of  $H$  in  $G$ .

(Or)

11 b) State and prove fundamental theorem of homomorphisms of groups.

12 a) Let  $S_n$  be the symmetric group on  $n$  symbols and let  $A_n$  be the group of even permutations. Then show that  $A_n$  is normal in  $S_n$  and  $O(A_n) = \frac{1}{2}(n!)$

(Or)

12 b) Prove that every subgroup of cyclic group is cyclic.

13 a) Prove that every finite integral domain is a field.

(Or)

13 b) Define principal ideal. Prove that every ideal of  $\mathbb{Z}$  is a principal ideal.

**BLUE PRINT FOR QUESTION PAPER PATTERN**  
**COURSE-IV, REAL ANALYSIS**

<b>Unit</b>	<b>TOPIC</b>	<b>S.A.Q(including choice)</b>	<b>E.Q(including choice)</b>	<b>Total Marks</b>
I	Real Number System and Real Sequence	2	2	30
II	Infinite Series	1	2	25
III	Limits and Continuity	1	2	25
IV	Differentiation and Mean Value Theorem	2	2	30
V	Riemann Integration	2	2	30
	<b>TOTAL</b>	8	10	140

**S.A.Q.** = Short answer questions (5 marks)

**E.Q.** = Essay questions (10 marks)

Short answer questions : 5 X 5 M = 25 M

Essay questions : 5 X 10 M = 50 M

.....  
Total Marks = 75 M  
.....

**CBCS/ SEMESTER SYSTEM**

(w.e.f. 2020-21 Admitted Batch)

**B.A./B.Sc. MATHEMATICS**

**COURSE-IV, REAL ANALYSIS**

**Time: 3Hrs**

**Max.Marks:75M**

**SECTION - A**

**Answer any FIVE questions. Each question carries FIVE marks 5 X 5  
M=25 M**

1. Prove that every convergent sequence is bounded.
2. Show that  $\lim\left(\frac{1}{(n+1)^2} + \frac{1}{(n+2)^2} + \dots + \frac{1}{(n+n)^2}\right) = 0$ .
3. Test the convergence of the series  $\sum_{n=1}^{\infty} (\sqrt[3]{n^3 + 1} - n)$ .
4. Examine for continuity of the function  $f$  defined by  $f(x) = |x| + |x - 1|$  at  $x=0$  and  $1$ .
5. Show that  $f(x) = x \sin \frac{1}{x}$ ,  $x \neq 0$ ;  $f(x) = 0$ ,  $x = 0$  is continuous but not derivable at  $x=0$ .
6. Verify Rolle's theorem for the function  $f(x) = x^3 - 6x^2 + 11x - 6$  on  $[1, 3]$ .
7. If  $f(x) = x^2 \forall x \in [0, 1]$  and  $p = \{0, \frac{1}{4}, \frac{2}{4}, \frac{3}{4}, 1\}$  then find  $L(p, f)$  and  $U(p, f)$ .
8. Prove that if  $f: [a, b] \rightarrow \mathbb{R}$  is continuous on  $[a, b]$  then  $f$  is  $\mathbb{R}$ - integrable on  $[a, b]$ .

**SECTION -B**

**Answer ALL the questions. Each question carries TEN marks. 5 X 10 M = 50 M**

9.(a) If  $S_n = 1 + \frac{1}{2!} + \frac{1}{3!} + \dots + \frac{1}{n!}$  then show that  $\{S_n\}$  converges.

(OR)

(b) State and prove Cauchy's general principle of convergence.

10.(a) State and Prove Cauchy's nth root test.

(OR)

(b) Test the convergence of  $\sum \frac{x^n}{x^n + a^n}$  ( $x > 0, a > 0$ ).

11.(a) Let  $f: \mathbb{R} \rightarrow \mathbb{R}$  be such that

$$f(x) = \frac{\sin(a+1)x + \sin x}{x} \text{ for } x < 0$$
$$= c \text{ for } x = 0$$

$$= \frac{(x+bx^2)^{1/2} - x^{1/2}}{bx^{3/2}} \text{ for } x > 0$$

Determine the values of  $a, b, c$  for which the function  $f$  is continuous at  $x=0$ .

(OR)

(b) Define uniform continuity, If a function  $f$  is continuous on  $[a, b]$  then  $f$  is uniformly continuous on  $[a, b]$

12.(a) Using Lagrange's theorem, show that  $x > \log(1+x) > \frac{x}{(1+x)} \forall x > 0$ .

(OR)

(b) State and prove Cauchy's mean value theorem.

13.(a) State and prove Riemann's necessary and sufficient condition for R- integrability.

(OR)

(b) Prove that  $\frac{\pi^3}{24} \leq \int_0^\pi \frac{x^2}{5+3\cos x} dx \leq \frac{\pi^3}{6}$ .

## BLUE PRINT FOR QUESTION PAPER PATTERN COURSE-V, LINEAR ALGEBRA

Unit	TOPIC	S.A.Q (including choice)	E.Q (including choice)	Marks Allotted
I	Vector spaces - I	2	2	30
II	Vector spaces - II	1	2	25
III	Linear Transformation	2	2	30
IV	Char. values and char. vectors	1	2	25
V	Inner product spaces	2	2	30
<b>Total</b>		<b>8</b>	<b>10</b>	<b>140</b>

**S.A.Q.** = Short answer questions (5 marks)

**E.Q.** = Essay questions (10 marks)

Short answer questions : 5 X 5 M = 25 M

Essay questions : 5 X 10 M = 50 M

.....  
Total Marks = 75 M  
.....

## CBCS/ SEMESTER SYSTEM

(w.e.f. 2020-21 Admitted Batch)

B.A./B.Sc. MATHEMATICS

COURSE-V, LINEAR ALGEBRA

Time: 3Hrs

Max.Marks:75M

### SECTION - A

Answer any **FIVE** questions. Each question carries **FIVE** marks **5 X 5 M=25 M**

1. Let  $p, q, r$  be fixed elements of a field  $F$ . Show that the set  $W$  of all triads  $(x, y, z)$  of elements of  $F$ , such that  $px+qy+rz=0$  is a vector subspace of  $V_3(R)$ .
2. Define linearly independent & linearly dependent vectors in a vector space. If  $\alpha, \beta, \gamma$  are linearly independent vectors of  $V(R)$  then show that  $\alpha + \beta, \beta + \gamma, \gamma + \alpha$  are also linearly independent.
3. Prove that every set of  $(n + 1)$  or more vectors in an  $n$  dimensional vector space is linearly dependent.
4. The mapping  $T : V_3(R) \rightarrow V_3(R)$  is defined by  $T(x, y, z) = (x-y, x-z)$ . Show that  $T$  is a linear transformation.
5. Let  $T: R^3 \rightarrow R^2$  and  $H: R^3 \rightarrow R^2$  be defined by  $T(x, y, z) = (3x, y+z)$  and  $H(x, y, z) = (2x-z, y)$ . Compute i)  $T+H$  ii)  $4T-5H$  iii)  $TH$  iv)  $HT$ .
6. If the matrix  $A$  is non-singular, show that the eigen values of  $A^{-1}$  are the reciprocals of the eigen values of  $A$ .
7. State and prove parallelogram law in an inner product space  $V(F)$ .
8. Prove that the set  $S = \left\{ \left( \frac{1}{3}, \frac{-2}{3}, \frac{-2}{3} \right), \left( \frac{2}{3}, \frac{-1}{3}, \frac{2}{3} \right), \left( \frac{2}{3}, \frac{2}{3}, \frac{-1}{3} \right) \right\}$  is an orthonormal set in the inner product space  $R^3(R)$  with the standard inner product.

### SECTION - B

Answer **ALL** the questions. Each question carries **TEN** marks. **5 X 10 M = 50 M**

- 9(a)) Define vector space. Let  $V(F)$  be a vector space. Let  $W$  be a non empty sub set of  $V$ . Prove that the necessary and sufficient condition for  $W$  to be a subspace of  $V$  is  $a, b \in F$  and  $\alpha, \beta \in V \Rightarrow a\alpha + b\beta \in W$ .



(OR)

(b) Prove that the four vectors  $(1,0,0)$ ,  $(0,1,0)$ ,  $(0,0,1)$  and  $(1,1,1)$  of  $V_3(\mathbb{C})$  form linearly dependent set, but any three of them are linearly independent.

10(a) Define dimension of a finite dimensional vector space. If  $W$  is a subspace of a finite dimensional vector space  $V(F)$  then prove that  $W$  is finite dimensional and  $\dim W \leq n$ .

(OR)

(b) If  $W$  be a subspace of a finite dimensional vector space  $V(F)$  then Prove that

$$\dim V/W = \dim V - \dim W.$$

11(a) Find  $T(x, y, z)$  where  $T: \mathbb{R}^3 \rightarrow \mathbb{R}$  is defined by  $T(1, 1, 1) = 3$ ,  $T(0, 1, -2) = 1$ ,  
 $T(0, 0, 1) = -2$

(OR)

(b) State and prove Rank Nullity theorem.

12(a) Find the eigen values and the corresponding eigen vectors of the matrix

$$A = \begin{pmatrix} 8 & -6 & 2 \\ -6 & 7 & -4 \\ 2 & -4 & 3 \end{pmatrix}.$$

(OR)

(b) State and prove Cayley-Hamilton theorem.

13(a) State and prove Schwarz's inequality in an Inner product space  $V(F)$ .

(OR)

(b) Given  $\{(2,1,3), (1,2,3), (1,1,1)\}$  is a basis of  $\mathbb{R}^3(\mathbb{R})$ . Construct an orthonormal basis using Gram-Schmidt orthogonalisation process.

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